

Class 2: Password security . v2

Note Title

Math objective for today: work out how long it takes to crack different types of passwords

[Go over syllabus .]

[Go over discussion questions from the lab]

① Cryptographic hash functions

A hash function is a computational procedure that creates a fingerprint of some data (e.g. a file, or a password). The fingerprint, or hash, has a fixed length.

↳ Also called digest, or checksum

example given any number, we output the last 2 digits. e.g. '157447' becomes '47'. This is a hash function, transforming a number of any length into a 2-digit hash.

A collision is when 2 different inputs hash to the same value

exercise : give an example of a collision for the above hash function.

A cryptographic hash function is a hash function for which no-one knows how to efficiently create collisions. (For a decent-sized hash, random guessing is not efficient — it would take billions of years to find a collision.)

Famous examples

see below for explanation

- MD5 - creates a 128-bit hash
 - published 1992
 - has been cracked and is not secure — collisions are known! See wikipedia page.
- SHA-256 - creates a 256-bit hash
 - published 2001
 - some weaknesses known, but still considered secure. See wikipedia.

Demo : Use web search to find an online SHA-256 calculator. Compute the SHA-256 hash of "Dickinson". How about "dickinson"?

The length of the hash is usually measured in bits or bytes. Bits are the 1s and 0s actually stored in a computer.

A byte is (roughly) the same thing as a character (like "a", "b", or "5" or "?") and it takes 8 bits to represent one byte. So a SHA-256 hash is 256 bits or 32 bytes or 32 characters. (or 64 hexadecimal digits, but don't worry if you don't know what this is).

(2) What are cryptographic hash functions used for?

Many, many things. One application is to verify passwords without storing them:

- computer does not store your password
- instead, stores (e.g. SHA-256) hash of your password
- when you enter your password, the computer calculates the hash and compares with stored version.

(3) Our attack model for password cracking + number of guesses needed

We assume a malicious hacker has obtained access to a system's file of password hashes. The hacker guesses passwords randomly, computing the hash of each one to see if it matches a hash on the system.

Number of guesses required, on average, is :

$$\text{avg num guesses} = \frac{1}{\text{num hashes} \times \text{prob of single correct guess}}$$

e.g. If password file has 50 hashes, and chance of correct guess is one-in-a-million, avg guesses needed is

$$1 / 50 \times \frac{1}{10^6} = \frac{10^6}{50} = 20,000.$$

Exercise: How many guesses are needed, on average, to crack one password from a file of 1000 hashes, if each guess succeeds with probability one-billionth?

Math help :

10^6 means $10 \times 10 \times \dots \times 10$

six times

↑ or 1 with 6 zeroes after it

i.e. 1,000,000 i.e. 1 million.

in typed text, sometimes written 10^6

④ Chance of success with a guess

Chance of success is just $\frac{1}{\text{num possibilities}}$

e.g. (a) for a password selected at random from a dictionary of 50,000 words, chance of success is $\frac{1}{50,000}$

(b) For a 4-digit PIN (ie. a numeric password),
number of possibilities is

$$10 \times 10 \times 10 \times 10 = 10^4 = 10,000$$

↗
num possibilities
for each digit

Chance of success is $\frac{1}{10,000}$.

(c) For a 6-letter alphabetic password (all lowercase),
num possibilities is

$$26 \times 26 \times \dots \times 26 = 26^6 \approx 300 \text{ million.}$$
$$= 3 \times 10^8$$

Chance of success is about $1/3 \times 10^8$

⑤ How long to crack?

A modern desktop computer can compute (very roughly)
100,000 hashes per second.

Average time to crack = $\frac{\text{avg num guesses needed}}{\text{num hashes per second}}$

Exercise: How long to crack a 6-letter lowercase password?

⑥ If time, discussin about this 100,000 hashes per second number:

- specialised machinery can be much faster
e.g. 'DES cracker' from 1998 did 10¹⁰ /sec.
- using multiple machines is faster
- how does this compare with the numbers from 6hr lab? If different, why?

⑦ If time, discuss some interesting results from the optional reading.

Source & further reading: Some of these notes are based on Smith, § 6.2-6.4.

That is a good place for additional information.