COMP 314 Homework Assignment 5

1. (14 points) For each of the problems given below, circle each complexity class the problem is known to be a member of.

| Problem | Complexity classes |
|-----------------------------------------------------|--------------------------------|
| ContainsWombat | Const Lin LogLin Quad Poly Exp |
| StartsWithWombat | Const Lin LogLin Quad Poly Exp |
| LISTALLTRIPLES | Const Lin LogLin Quad Poly Exp |
| Factor | Const Lin LogLin Quad Poly Exp |
| TRAVELINGSALESMAN | Const Lin LogLin Quad Poly Exp |
| EASTWARDTRAVELINGSALESMAN | Const Lin LogLin Quad Poly Exp |
| AlwaysYes | Const Lin LogLin Quad Poly Exp |
| HALTSINEXPTIME | Const Lin LogLin Quad Poly Exp |
| HaltsOnEmpty | Const Lin LogLin Quad Poly Exp |
| Input is a Python program, output is the num- | Const Lin LogLin Quad Poly Exp |
| ber of lines in the program | |
| Input is a list of numbers, output is the largest | Const Lin LogLin Quad Poly Exp |
| number in the list | |
| Input is a list of numbers, output is a list of all | Const Lin LogLin Quad Poly Exp |
| pairs of distinct numbers in the list | |
| Input is a list of numbers, output is the number | Const Lin LogLin Quad Poly Exp |
| of unique numbers in the list | |
| Input is single number n , output is the letter | Const Lin LogLin Quad Poly Exp |
| "x" repeated n times | |

2. (10 points) What is "the" complexity of the following Python program? Give a reasonably detailed explanation of your answer.

3. (a) (15 points) Write a computer program, using the programming language of your choice, that takes as input a list of words separated by space characters. (Here, a *word* is any alphanumeric string.) The output is a list of all possible permutations of the input words, with each permutation printed on a separate line. For example, if the input is "apple banana grape32", the output is:

apple banana grape32 apple grape32 banana banana apple grape32 banana grape32 apple grape32 apple banana grape32 banana apple

(Of course, your program might print these lines in a different order.) Your program does not have to read its input from a text file. You can hardwire the input into the program, e.g. input = "apple banana grape32". Hint: use recursion.

(b) (5 points) What is "the" complexity of the program you wrote for part (a)? Briefly justify your answer.

4. (a) (15 points) Write a computer program, using the programming language of your choice, that takes as input a list of words separated by space characters. (Here, a *word* is again any alphanumeric string.) The output is a list of all possible ordered pairs of the input words, with each pair printed on a separate line. For example, if the input is "apple banana grape32", the output is:

```
apple apple
apple banana
apple grape32
banana apple
banana banana
banana grape32
grape32 apple
grape32 banana
grape32 grape32
```

(Of course, your program might print these lines in a different order.) As in the previous question, feel free to hardwire the input into your program.

(b) (5 points) What is "the" complexity of the program you wrote for part (a)? Briefly justify your answer.

5. (5 points) Suppose the complexity of problem X is $O(n^6)$, the complexity of problem Y is $O(n^2)$. Consider a new problem W. Given an input of length n, we can

solve W by first solving n instances of X that each have length \sqrt{n} , then solving an instance of Y that has length n. What is "the" complexity of W? What complexity classes does W belong to? Justify your answer.

6. (5 points) Suppose the complexity of problem X is $O(n^3)$, the complexity of problem Y is $O(n \log n)$, and the complexity of problem Z is $O(3^n)$. Consider a new problem W. Given an input of length n, we can solve W by first solving an instance of X that has length n/2, then solving an instance of Y that has length n/2, then solving an instance of Y that has length n/2, then solving an instance of Z that has the fixed length 5. What is "the" complexity of W? What complexity classes does W belong to? Justify your answer.